

For an oscillating electric dipole, $\mathbf{H} = \frac{ck^2}{4\pi} \frac{e^{ikr}}{r} \hat{\mathbf{r}} \times \mathbf{p}$, $\mathbf{E} = -Z_0 \hat{\mathbf{r}} \times \mathbf{H}$, the time-averaged power per solid angle is

$$\begin{aligned}
 \frac{dP}{d\Omega} &= \text{Re} \left[r^2 \hat{\mathbf{r}} \cdot \frac{1}{2} \mathbf{E} \times \mathbf{H}^* \right] = \text{Re} \left[r^2 \hat{\mathbf{r}} \cdot \frac{1}{2} (-Z_0 \hat{\mathbf{r}} \times \mathbf{H}) \times \mathbf{H}^* \right] \\
 &= \frac{Z_0 r^2}{2} \text{Re} \{ \hat{\mathbf{r}} \cdot [\mathbf{H}^* \times (\hat{\mathbf{r}} \times \mathbf{H})] \} \\
 &= \frac{Z_0 r^2}{2} \text{Re} \{ \hat{\mathbf{r}} \cdot [\hat{\mathbf{r}}(\mathbf{H}^* \cdot \mathbf{H}) - \mathbf{H}(\hat{\mathbf{r}} \cdot \mathbf{H}^*)] \} \quad \leftarrow \hat{\mathbf{r}} \cdot \mathbf{H}^* \propto \hat{\mathbf{r}} \cdot (\hat{\mathbf{r}} \times \mathbf{p}^*) = 0 \\
 &= \frac{Z_0 r^2}{2} |\mathbf{H}|^2 = \frac{Z_0 r^2}{2} \left| \frac{ck^2}{4\pi} \frac{e^{ikr}}{r} \hat{\mathbf{r}} \times \mathbf{p} \right|^2 = \frac{Z_0 c^2 k^4}{32\pi^2} |\hat{\mathbf{r}} \times \mathbf{p}|^2 \\
 &= \frac{Z_0 c^2 k^4}{32\pi^2} |\mathbf{p}|^2 \sin^2 \theta.
 \end{aligned}$$

The total power is

$$\begin{aligned}
 P &= \int \frac{dP}{d\Omega} d\Omega = \frac{Z_0 c^2 k^4}{32\pi^2} |\mathbf{p}|^2 \iint \sin^2 \theta \sin \theta d\theta d\phi \quad \leftarrow z = \cos \theta \\
 &= \frac{Z_0 c^2 k^4}{32\pi^2} |\mathbf{p}|^2 \cdot 2\pi \cdot \int_{-1}^1 (1 - z^2) dz \\
 &= \frac{Z_0 c^2 k^4}{12\pi^2} |\mathbf{p}|^2
 \end{aligned}$$